# Electron Exchange between $\operatorname{Bis}\left(\eta^{6}\right.$-arene)chromium(I) and $\operatorname{Bis}\left(\eta^{6}\right.$-arene $)$ chromium $(0)$. Comparisons between Experimental and Calculated Kinetics Parameters 

Tomi T.-T. Li, Michael J. Weaver,* and Carl H. Brubaker, Jr.*<br>Contribution from the Department of Chemistry, Michigan State University, East Lansing, Michigan 48824. Received July 20, 1981


#### Abstract

Comparisons have been made between kinetics parameters for the self-exchange of $\left(\eta^{6}-\operatorname{arene}\right)_{2} \mathrm{Cr}^{1} /\left(\eta^{6}-\operatorname{arene}\right)_{2} \mathrm{Cr}^{0}$ (where arene = benzene, toluene, methoxybenzene, biphenyl, ethyl benzoate, and chlorobenzene) measured by ESR line broadening in dimethyl sulfoxide and the predictions from contemporary electron-transfer theory. The biphenyl system was additionally studied in a number of other solvents. These reactions provide especially tractable systems with which to test theories of outer-sphere electron transfer since the work terms should be essentially zero and the inner-shell contributions $\Delta G^{*}$ in to the free energy barrier are small and can be estimated from infrared spectroscopy combined with crystallographic data. The solvent dependence of the rate constants for $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{C}_{6} \mathrm{H}_{5}\right)_{2} \mathrm{Cr}^{1 / 0}$ self-exchange was found to be in reasonable agreement with the predictions of the dielectric continuum model. Frequency factors were derived from the experimental rate constants coupled with the estimates of $\Delta G^{*}{ }_{\text {in }}$ and values of the outer-shell contribution $\Delta G^{*}$ out obtained by using the dielectric continuum model. These were found to be somewhat (ca. 5-20-fold) larger than the corresponding frequency factors derived from the experimental activation enthalpies combined with the dielectric continuum estimates of the activation entropies. These "experimental" frequency factors are compared with the estimates obtained from the "reactive collision" and the "ion-pair preequilibrium" models. The majority of the experimental frequency factors were found to be numerically closer to the predictions of the former model. However, the experimental values were found to decrease substantially with the addition of substituents on the arene ring, indicating the importance of steric effects. It is suggested that the discrepancies between the experimental results and the predictions of the preequilibrium model observed for these and other systems may be due to a combination of steric and nonadiabatic effects.


Outer-sphere electron-exchange reactions constitute an especially interesting class of chemical reactions in solution in that it is anticipated that quantitative theoretical descriptions of the reaction dynamics can be provided in many cases. Theoretical treatments of varying levels of complexity (and usefulness) have been developed that allow detailed insight into the physical processes involved. ${ }^{1}$ Some recent treatments outline a useful framework within which various aspects of the theories may be tested by comparison with experimental data. ${ }^{2-4}$

One question that has arisen is the choice of the frequency factor for outer-sphere reactions. ${ }^{2,3}$ Two alternative models have been proposed. ${ }^{2}$ The "reactive collision" model considers that electron transfer occurs upon collision between appropriately energetic reactants, leading to the formulation

$$
\begin{equation*}
k=\kappa \Gamma_{\mathrm{n}} Z\left[\exp (-w / R T) \exp \left(-\Delta G^{*} / R T\right)\right] \tag{1}
\end{equation*}
$$

where $k$ is the observed (second order) rate constant for electron exchange, $\kappa$ is the electronic transmission coefficient, $\Gamma_{n}$ is a nuclear tunneling factor, $Z$ is the collision frequency, $w$ is the work required to form the collision complex from the separated reactants, and $\Delta G^{*}$ is the free energy of activation for the elementary elec-tron-transfer step. ${ }^{2,3}$ The alternative "preequilibrium" model considers that reaction occurs by activation within a previously formed bimolecular assembly. 2,3 This leads to the expression

$$
\begin{equation*}
k=\kappa \Gamma_{\mathrm{n}} K_{\mathrm{p}}{ }^{\circ} \nu_{\mathrm{p}}\left[\exp (-w / R T) \exp \left(-\Delta G^{*} / R T\right)\right] \tag{2}
\end{equation*}
$$

where $K_{\mathrm{p}}{ }^{\circ}$ is the equilibrium constant for formation of the "precursor complex" in the absence of work terms (i.e., when $w$ $=0$ ), $\nu_{\mathrm{p}}$ is the frequency factor for activation within the precursor

[^0]complex, and the other terms have the same significance as in eq 1. These two formulations therefore differ in the overall preexponential factor in that the "classical" frequency factor $A$ equals the collision frequency $Z$ in eq 1 but is replaced by the composite term $K_{\mathrm{p}}{ }^{\circ} \nu_{\mathrm{p}}$ in eq 2. Although the collision formulation is most commonly employed for bimolecular solution reactions, including electron-transfer processes, the preequilibrium model may provide a more appropriate description of outer-sphere electron transfer when the reaction is expected to take place via electron tunneling between weakly interacting species.

Comparisons between the predictions of eq 1 and 2 with experimental data can be made by obtaining estimates of the frequency factor $A$ in two ways. First, the observed rate constant at a given temperature can be combined with theoretical values of $\Delta G^{*}, w, \kappa$, and $\Gamma_{\mathrm{n}}$ to yield estimates of $A$ (method a). Second, the Arrhenius activation energy, $E_{\mathrm{a}}$, derived from the observed temperature dependence of $k$, can be corrected for the temperature dependences of $\kappa, \Gamma_{n}$, and $A$ to yield an "experimental value" of the enthalpic component of $\Delta G^{*}, \Delta H^{*}$. Values of $A$ can then be found by combining this value of $\Delta H^{*}$ and a value of $k$ at a given temperature with theoretical estimates of $\Delta S^{*}, w, \kappa$, and $\Gamma_{n}$ (method b). Since both methods depend critically upon the assumed values of $\Delta G^{*}$ or $\Delta S^{*}, w, \kappa$, and $\Gamma_{n}$, it is clearly important to select systems for which these parameters can be estimated with confidence. Suitable redox couples will therefore be those for which the structural differences between the oxidized and the reduced form are known, and preferably small, so that the in-ner-shell contribution to $\Delta G^{*}$ can be calculated and $\Gamma_{n}$ will be close to unity. ${ }^{4}$ Additionally, it is desirable that the reactants be spherical, or nearly so, and the product of the reactant charges be small so that the work term, $w$, is small and the outer-shell (solvent) contribution to $\Delta G^{*}$ is most likely to conform to the prediction of the conventional dielectric continuum model.

Several tests of eq 1 and 2 have recently been made. Brown and Sutin ${ }^{2}$ studied the self-exchange of $\mathrm{Ru}(\mathrm{III}) / \mathrm{Ru}(\mathrm{II})$ couples containing polypyridine and/or ammine ligands in aqueous solution. Better agreement between the experimental rate constants and activation parameters was obtained by using the reactive collision rather than the preequilibrium formulation. Similar findings were reported by Meyer et al. in a study of electron

Table I. Calculated Reorganization Energies and Related Parameters for the Self-Exchange of Bis $\left(\eta^{6}\right.$-arene)chromium(I)/(0) in $\mathrm{Me}_{2} \mathrm{SO}$ at $22^{\circ} \mathrm{C}$

|  | arene |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{C}_{6} \mathrm{H}_{6}$ | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CH}_{3}$ | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{OCH}_{3}$ | $\left(\mathrm{C}_{6} \mathrm{H}_{5}\right)_{2}$ | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{COOC}_{2} \mathrm{H}_{5}$ | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Cl}$ |
| $r, \AA^{a}$ | 7.3 | 8.4 | 7.8 | 11.6 | 9.6 | 8.6 |
| $\Delta a, \AA$ | 0.07 | 0.06 | 0.08 | 0.07 | 0.04 | 0.04 |
| $\nu_{1}{ }^{\text {a }}, \nu_{0}{ }^{\text {a }}, \mathrm{cm}^{-1}$ | 490, 466 | 489, 470 | 490, 464 | 489, 465 | 480, 468 | 481, 468 |
| $\Delta G_{\text {in }}(T), \mathrm{kcal} \cdot \mathrm{mol}^{-1} \mathrm{~b}$ | 1.15 | 0.85 | 1.55 | 1.30 | 0.45 | 0.50 |
| $\Delta G^{*}$ out, $\mathrm{kcal} \cdot \mathrm{mol}^{-1} \mathrm{c}$ | 4.9 | 4.3 | 4.6 | 3.1 | 3.8 | 4.2 |
| $\Delta G^{*}$ calcd, $\mathrm{kcal} \cdot \mathrm{mol}^{-1} d$ | 6.1 | 5.2 | 6.2 | 4.4 | 4.3 | 4.7 |
| $\Delta S^{*}$ calcd, ${ }^{\text {cal }} \cdot \mathrm{deg}^{-1} \cdot \mathrm{~mol}^{-1} e$ | -1.0 | -0.9 | -1.2 | -0.9 | -0.8 | -0.8 |

${ }^{a}$ The average "side-by-side" internuclear distance ( $\mathrm{Cr}^{0}-\mathrm{Cr}^{+}$) as estimated from molecular models. ${ }^{b}$ Calculated using eq 3. ${ }^{c}$ Calculated using eq 4. Sources for dielectric constants: $D_{\text {op }}$, ref $22 ; D_{\mathrm{s}}$, ref 21 . ${ }^{d}$ The sum of $\Delta G^{*}{ }_{\text {in }}(T)$ and $\Delta G^{*}$ out. $e$ The sum of $\Delta S^{*}$ in $(T)$ and $\Delta S^{*}$ out. $\Delta S^{*}{ }_{\text {in }}(T)$ is taken from the temperature derivative of $\Delta G^{*}{ }_{\mathrm{in}}(T): \Delta S^{*}{ }_{\mathrm{in}}(T)=-\left[\mathrm{d} \Delta G^{*}{ }_{\text {in }}(T) / \mathrm{d} T\right]=-\left[\Delta G^{*}{ }_{\text {in }}(T) / T\right]\left[1-\left(h \nu_{\mathrm{in}} / 2 k T\right)\right.$ $\left.\operatorname{csch}\left(h \nu_{\mathrm{in}} / 2 k T\right)\right]$, where $\nu_{\text {in }}$ is the average frequency of inner-shell motion (symmetric stretch), from $\nu_{\text {in }}=\left[2 \nu_{0}^{2} \nu_{1}^{2} /\left(\nu_{0}^{2}+\nu_{1}^{2}\right)\right]^{1 / 2} \quad \Delta S^{*}$ out is calculated from eq 6 using values of $\mathrm{d} D_{\mathrm{op}} / \mathrm{d} T$ and $\mathrm{d} D_{\mathbf{s}} / \mathrm{d} T$ obtained from sources given in footnote $c$.
exchange of $\left[\mathrm{Ru}_{3} \mathrm{O}\left(\mathrm{CH}_{3} \mathrm{CO}_{2}\right)_{6}(\mathrm{py})_{3}\right]^{+/ 0}$ in dichloromethane. ${ }^{5}$ Systems of this latter type, where one form of the redox couple is uncharged, have the important advantage that the electrostatic work required to form the encounter complex should be essentially zero.

We have recently reported rate constants and activation parameters for the self-exchange of various ( $\eta^{6}$-arene) ${ }_{2} \mathrm{Cr}^{+/ 0}$ couples, $\mathrm{Cr}\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{X}\right)_{2}{ }^{+/ 0}$, where $\mathrm{X}=\mathrm{H}, \mathrm{CH}_{3}, \mathrm{OCH}_{3}, \mathrm{C}_{6} \mathrm{H}_{5}, \mathrm{COOC}_{2} \mathrm{H}_{5}$, or Cl , in dimethyl sulfoxide ( $\mathrm{Me}_{2} \mathrm{SO}$ ), by using the ESR linebroadening technique. ${ }^{6}$ The self-exchange of $\mathrm{Cr}\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{C}_{6} \mathrm{H}_{5}\right)_{2}{ }^{+/ 0}$ was additionally studied in six other solvents. These reactants provide especially suitable systems with which to test models of outer-sphere electron transfer. Besides the likely absence of electrostatic work terms, they have the advantage that the in-ner-shell components $\Delta G^{*}$ in are small and can be calculated from appropriate structural data. The comparison of rate constants and activation parameters for such a series of redox couples with various ring substituents can therefore provide a means of exploring the influence of reactant asymmetry on the frequency factors for electron exchange. Such comparisons between the experimental rate parameters and the predictions of eq 1 and 2 are given in the present report.

## Experimental Section

The syntheses of all bis( $\eta^{6}$-arene)chromium compounds were described in ref 6 . Infrared spectra were obtained by means of a Perkin-Elmer 457 spectrometer by using either KBr pellets or Nujol mulls at room temperature. The reported IR frequencies are accurate to $\pm 0.5 \mathrm{~cm}^{-1}$. The Nujol mulls of the air-sensitive $\mathrm{Cr}(0)$ complexes were prepared in an argon-filled drybox, and the spectra were measured in an argon atmosphere.

## Results and Discussion

Reorganization Energies. The contribution to $\Delta G^{*}$ arising from inner-shell reorganization, $\Delta G^{*}{ }_{\text {in }}(T)$, for each self-exchange reaction was calculated by means of the expression ${ }^{7}$

$$
\begin{equation*}
\Delta G_{i \mathrm{in}}^{*}(T)=\frac{2 n f_{0} f_{1}(\Delta a)^{2} k_{\mathrm{B}} T}{f_{0} y_{1}+f_{1} y_{0}} \tag{3}
\end{equation*}
$$

In eq $3, f_{0}$ and $f_{1}$ are the force constants for the metal-arene bonds in the $\mathrm{Cr}^{0}$ and $\mathrm{Cr}^{1}$ oxidation states, $\Delta a$ is the difference in the corresponding equilibrium bond distances, $n$ is the number of metal-ligand bonds involved, and $y_{i}=h v_{i} \operatorname{coth}\left(h v_{i} / 4 k_{\mathrm{B}} T\right)$, where $\nu_{i}$ are the observed Cr -arene stretching frequencies for the oxidation state $i$. [Equation 3 takes into account the nuclear tunneling factor $\Gamma_{\mathrm{n}}$ at a given temperature; thus $\Delta G^{*}{ }_{\text {in }}(T)$ is related to the classical inner-shell reorganization energy $\Delta G^{*}{ }_{\text {in }}$ by $\Delta G^{*}(T)=$ $\Delta G^{*}{ }_{\mathrm{in}}-R T \ln \Gamma_{\mathrm{n}}{ }^{4}$ However, $\Gamma_{\mathrm{n}}$ is close to unity (1.0-1.2) for the present systems.] The normal vibrations of $\operatorname{Cr}\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)_{2}$ and

[^1]$\mathrm{Cr}\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)_{2}{ }^{+}$have been assigned to be of $D_{6 h}$ symmetry from the infrared spectra, ${ }^{8}$ so $n$ can be set equal to 2 . The force constants $f_{0}$ and $f_{1}$ in eq 3 refer to the symmetrical stretching vibration of the two arene rings with respect to the chromium atom. The frequencies of these symmetrical vibrations, $\nu_{0}$ and $\nu_{1}$, have been determined for the $\mathrm{Cr}\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)_{2}{ }^{+/ 0}$ couple to be about $270 \mathrm{~cm}^{-1}$ and $279 \mathrm{~cm}^{-1}$, respectively ${ }^{8 \mathrm{c}}$ allowing the force constants to be determined from $f=5.89 \times 10^{-2} \nu m_{\mathrm{Y}}$, where $m_{\mathrm{Y}}$ is the mass of one arene ring. Value of $\nu_{0}$ and $\nu_{1}$ for the other arenes studied here are unavailable. However, they are unlikely to be greatly different from those for $\mathrm{Cr}\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)_{2}{ }^{+/ 0}$; thus the asymmetrical $\mathrm{Y}-\mathrm{Cr}-\mathrm{Y}$ stretching frequencies $\nu_{0}{ }^{\text {a }}$ and $\nu_{1}{ }^{\text {a }}$ are within $5-10 \mathrm{~cm}^{-1}$ for all the $\mathrm{Cr}(\mathrm{I})$ and $\mathrm{Cr}(0)$ arenes (Table I$)$. The values of $f_{0}$ and $f_{1}$ were therefore estimated by assuming that $\nu_{0}=270 \mathrm{~cm}^{-1}$ and $\nu_{1}=279$ $\mathrm{cm}^{-1}$.

The value of $\Delta a$ is $0.07 \AA$ for the $\mathrm{Cr}\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)_{2}{ }^{+/ 0}$ couple as found from X-ray crystallographic data. ${ }^{9}$ For the other $\mathrm{Cr}(\mathrm{I}) / \mathrm{Cr}(0)$ couples, estimates were obtained from the corresponding difference in infrared stretching frequencies by assuming that $\Delta a \propto f_{0}{ }^{\text {a }}-$ $f_{1}^{\mathrm{a}}$, where $f_{0}^{\mathrm{a}}$ and $f_{1}^{\mathrm{a}}$ are the force constants for the asymmetric vibrations obtained from $\nu_{0}{ }^{a}$ and $\nu_{1}{ }^{\text {a }}$ by using the formula $f^{a}=$ $5.89 \times 10^{-2}\left(\nu^{2}\right)^{2}\left[m_{\mathrm{C}_{\mathrm{r}}} m_{\mathrm{Y}} /\left(m_{\mathrm{C}_{\mathrm{r}}}+2 m_{\mathrm{Y}}\right)\right]$, where $m_{\mathrm{C}_{\mathrm{r}}}$ is the mass of the chromium atom. ${ }^{8, \mathrm{c}, \mathrm{c}}$ The required proportionality constant was determined from the experimental data for $\mathrm{Cr}\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)_{2}{ }^{+10}$. Justification for this procedure is available for metallocenes. ${ }^{10}$ The estimates of $\Delta G^{*}$ in $(T)$ resulting from inserting the appropriate values of $f_{0}, f_{1}$, and $\Delta a$ into eq 3 are given in Table I. It is seen that the values of $\Delta G^{*}{ }_{\text {in }}(T)$ are mostly below $1-1.5 \mathrm{kcal} \cdot \mathrm{mol}^{-1}$, indicating that inner-shell reorganization provides only a small contribution to the electron-transfer barrier. This is expected since the orbital into which the electron is transferred, $a_{1 \mathrm{~g}}$ having $d_{z^{2}}$ symmetry, is essentially nonbonding ${ }^{11}$ so that it may contain one or two electrons [as in $\mathrm{Cr}(\mathrm{I})$ and $\mathrm{Cr}(0)$, respectively] with little change in the metal-arene bonding.

The other contribution to $\Delta G^{*}$ is provided by the "outer-shell" reorganization energy of the surrounding solvent, $\Delta G^{*}{ }_{\text {out }}$. This component was calculated by using the dielectric continuum expression ${ }^{12}$

$$
\begin{equation*}
\Delta G^{*}{ }_{\mathrm{out}}=\frac{e^{2}}{4}\left(\frac{1}{2 a_{1}}+\frac{1}{2 a_{2}}-\frac{1}{r}\right)\left(\frac{1}{D_{\mathrm{op}}}-\frac{1}{D_{\mathrm{s}}}\right) \tag{4}
\end{equation*}
$$

where $D_{\mathrm{op}}$ and $D_{\mathrm{s}}$ are the optical and static dielectric constants, respectively, $a_{1}$ and $a_{2}$ are the radii of the two (spherical) reactants, $r$ is the distance between the two reacting centers in the activated state, and $e$ is the electronic charge. For the reactions considered
(8) (a) Johns, L. H. "Inorganic Vibrational Spectroscopy"; Marcel Dekker: New York, 1971; p 175. (b) Maslowsky, E., Jr. "Vibrational Spectra of Organometallic Compounds"; Wiley-Interscience: New York, 1977; p 301. (c) Fritz, H. P. Adv. Organomet. Chem. 1964, l, 239.
(9) (a) Kenlen, E.; Jellinek, F. J. Organomet. Chem. 1966, 5, 490 . (b) Starovskii, O. V.; Strichkov, Y. T. Dokl. Akad. Nauk SSSR 1961, 135, 620. (10) Haaland, A. Acc. Chem. Res. 1979, 12, 415.
(11) Anderson, S. E., Jr.; Drago, R. S. Inorg. Chem. 1972, 11, 1564. (12) Marcus, R. A. J. Chem. Phys. 1965, 43, 679.

Table II. Comparison of Experimental and Calculated Enthalpies of Activation for the Self-Exchange of
$\operatorname{Bis}\left(\eta^{6}\right.$-arene) chromium(I)/(0) in $\mathrm{Me}_{2} \mathrm{SO}$ at $22^{\circ} \mathrm{C}$

| arene | $\begin{gathered} 10^{-7} k \\ \mathrm{M}^{-1} \\ \mathrm{~s}^{-1} a \end{gathered}$ | exptl |  | calcd |
| :---: | :---: | :---: | :---: | :---: |
|  |  | $\begin{aligned} & \Delta H^{*} \mathrm{pe}, \\ & \mathrm{kcal} \cdot \\ & \mathrm{~mol}^{-1} \mathrm{~b} \end{aligned}$ | $\begin{aligned} & \Delta H_{\mathrm{rc}}^{*}, \\ & \mathrm{kcal}^{\prime} \\ & \mathrm{mol}^{-1} c \end{aligned}$ | $\begin{gathered} \Delta H^{*} \text { calcd } \\ \text { kcal } \\ \mathrm{mol}^{-1} d \end{gathered}$ |
| $\mathrm{C}_{6} \mathrm{H}_{6}$ | 6.0 | 4.0 | 3.7 | 5.7 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CH}_{3}$ | 3.3 | 4.6 | 4.3 | 5.0 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{OCH}_{3}$ | 7.7 | 3.6 | 3.3 | 5.8 |
| $\left(\mathrm{C}_{6} \mathrm{H}_{5}\right)_{2}$ | 23 | 2.6 | 2.3 | 4.2 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{COOC}_{2} \mathrm{H}_{5}$ | 32 | 2.3 | 2.0 | 4.1 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Cl}$ | 20 | 2.9 | 2.6 | 4.4 |

${ }^{a}$ Experimental rate constant, taken from ref $6 .{ }^{\dot{b}}$ Obtained from $\Delta H^{*}{ }_{\mathrm{pe}}=E_{\mathrm{a}}$, where $E_{\mathrm{a}}$ is the Arrhenius activation energy. ${ }^{\mathrm{c}}$ Obtained from $\Delta H^{*}{ }_{\mathrm{rc}}=E_{\mathrm{a}}-0.5 R T .{ }^{d}$ Calculated enthalpies of activation, obtained from $\Delta H^{*}$ calcd $=\Delta G^{*}$ calcd $+T \Delta S^{*}$ calcd using values of $\Delta G^{*}$ calcd and $\Delta S^{*}$ calcd given in Table I.
here, it is reasonable to assume that approximately $r=2 a_{1}=2 a_{2}$ so that eq 4 reduces to

$$
\begin{equation*}
\Delta G_{\mathrm{out}}^{*}=\frac{e^{2}}{4 r}\left(\frac{1}{D_{\mathrm{op}}}-\frac{1}{D_{\mathrm{s}}}\right) \tag{5}
\end{equation*}
$$

The values of $r$ for each reaction were calculated by assuming that the transition state is formed with the two reactants placed "side by side" (i.e., with the arene rings lying in the same plane) ${ }^{6}$ and by using the reported bond distances and van der Waals radii. ${ }^{9,13}$ These estimates of $r$ and the resulting values of $\Delta G^{*}{ }_{\text {out }}$ obtained from eq 4 by using known values of $D_{\text {op }}$ and $D_{5}$ are given in Table I (see footnotes for data sources). Also listed in Table I are the calculated values of $\Delta G^{*}, \Delta G^{*}$ calcd, obtained for each reaction from the sum of the corresponding values of $\Delta G^{*}{ }_{\text {in }}$ and $\Delta G^{*}{ }_{\text {out }}$.

In addition to the free energies of reorganization, it is also necessary to calculate values of the enthalpic and entropic components of $\Delta G^{*}, \Delta H^{*}$ and $\Delta S^{*}$, respectively. The outer-shell component of $\Delta S^{*}, \Delta S^{*}$ out, was determined from the temperature derivative of $\Delta G^{*}{ }_{\text {out }}$ :
$\Delta S^{*}{ }_{\text {out }}=-\left(\frac{\mathrm{d} \Delta G_{\text {out }}^{*}}{\mathrm{~d} T}\right)=\frac{e^{2}}{4 r}\left(\frac{1}{D_{\mathrm{op}}{ }^{2}} \frac{\mathrm{~d} D_{\mathrm{op}}}{\mathrm{d} T}-\frac{1}{D_{\mathrm{s}}{ }^{2}} \frac{\mathrm{~d} D_{\mathrm{s}}}{\mathrm{d} T}\right)$
The inner-shell component of $\Delta S^{*}, \Delta S^{*}{ }_{\mathrm{in}}$, was calculated from the temperature derivative of $\Delta G^{*}$ in $(T)$ (eq 3 ), thereby taking into account the (small) temperature dependence of $\Gamma_{n}{ }^{4}$ The resulting values of $\Delta S^{*}{ }_{\text {in }}(-0.3$ to $-0.6 \mathrm{eu})$ were then summed with the corresponding estimates of $\Delta S^{*}{ }_{\text {out }}$ to yield the calculated activation entropies $\Delta S^{*}$ calcd listed in Table I.

Comparison of Experimental and Theoretical Kinetics Parameters. As noted in the introduction, tests of the applicability of eq 1 or 2 to describe the experimental kinetics parameters can be made either by combining the experimental rate constant at a given temperature with a theoretical estimate of $\Delta G^{*}$ (method a) or by employing both the rate constant and its temperature derivative along with a theoretical estimate of $\Delta S^{*}$ (method b). The resulting "experimental" frequency factors can be compared with the values of $Z$ and $K_{\mathrm{p}}{ }^{\circ} \nu_{\mathrm{p}}$ calculated by using various models. Alternatively, the calculated frequency factors can be combined with the observed rate constant and activation parameters to yield "experimental" values of $\Delta G^{*}$ and $\Delta S^{*}$, which can be compared with the corresponding theoretical estimates. Clearly, the reliability with which a given model for calculating frequency factors can be tested depends sensitively on the accuracy with which $\Delta G^{*}$ or $\Delta S^{*}$ can be calculated, and vice versa. However, the experimental enthalpies of activation $\Delta H^{*}$ obtained from the temperature dependence of the rate constants are insensitive to the

[^2]Table III. Comparison of Calculated and 'Experimental''
Frequency Factors $\left(\mathrm{M}^{-1} \cdot \mathrm{~s}^{-1}\right)$ for the Self-Exchange of $\operatorname{Bis}\left(\eta^{6}\right.$-arene)chromium(I)/(0) in $\mathrm{Me}_{2} \mathrm{SO}$ at $22{ }^{\circ} \mathrm{C}$

| arene | calcd freq factors |  | "exptl" freq factors |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} A^{\text {pe }}{ }_{\text {calcà }} \\ (\mathrm{eq} 8) \end{gathered}$ | $\begin{gathered} A^{\mathrm{rc}} \mathrm{calcd} \\ (\mathrm{eq} 9) \end{gathered}$ | $\begin{gathered} A_{\mathrm{a}} \\ (\mathrm{eq} 7 \mathrm{a}) \end{gathered}$ | $\begin{gathered} A_{\mathrm{b}} \\ (\mathrm{eq} 7 \mathrm{~b}) \end{gathered}$ |
| $\mathrm{C}_{6} \mathrm{H}_{6}$ | $3.5 \times 10^{12}$ | $2.5 \times 10^{11}$ | $1.7 \times 10^{12}$ | $9.1 \times 10^{10}$ |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CH}_{3}$ | $5.3 \times 10^{12}$ | $3.1 \times 10^{11}$ | $2.4 \times 10^{11}$ | $1.3 \times 10^{11}$ |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{OCH}_{3}$ | $5.9 \times 10^{12}$ | $2.5 \times 10^{11}$ | $2.8 \times 10^{12}$ | $6.5 \times 10^{10}$ |
| $\left(\mathrm{C}_{6} \mathrm{H}_{5}\right)_{2}$ | $1.7 \times 10^{13}$ | $4.7 \times 10^{11}$ | $4.5 \times 10^{11}$ | $3.1 \times 10^{10}$ |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{COOC}_{2} \mathrm{H}_{5}$ | $9.1 \times 10^{12}$ | $3.3 \times 10^{11}$ | $4.9 \times 10^{11}$ | $2.4 \times 10^{10}$ |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Cl}$ | $6.2 \times 10^{12}$ | $3.0 \times 10^{11}$ | $6.1 \times 10^{11}$ | $4.2 \times 10^{10}$ |

particular model employed for the frequency factor. Therefore the comparison between the experimental and calculated values of $\Delta H^{*}$ provides a useful independent test of the likely validity of such theoretical reorganization parameters.

Table II contains a comparison of experimental and calculated values of $\Delta H^{*}$ for the various $\mathrm{Cr}(\mathrm{I}) / \mathrm{Cr}(0)$ self-exchange reactions in $\mathrm{Me}_{2} \mathrm{SO}$. Two "experimental" values of $\Delta H^{*}$ are listed for each reaction. The first type, labeled $\Delta H^{*}{ }_{p e}$, is equal to the Arrhenius activation energy, $E_{\mathrm{a}}=R[\partial \ln k / \partial(1 / T)]$; these values are consistent with the preequilibrium formulation since the preexponential factor in this model $\left(\kappa \Gamma_{\mathrm{n}} K_{\mathrm{p}}{ }^{\circ} \nu_{\mathrm{p}}\right.$, eq 2$)$ is expected to be essentially independent of temperature. The second type, labeled $\Delta H^{*}{ }_{\mathrm{rc}}$, is uniformly $0.3 \mathrm{kcal} \cdot \mathrm{mol}^{-1}(=R T / 2)$ smaller than $\Delta H_{\mathrm{pe}}^{*}$; these correspond to the use of the reactive collision formulation since the collision frequency $Z$ appearing in eq 1 is expected to be proportional ${ }^{2}$ to $T^{1 / 2}$. The calculated values of $\Delta H^{*}$, labeled $\Delta H^{*}$ calcd in Table II, were obtained from the corresponding values of $\Delta G^{*}$ caled and $\Delta S^{*}$ calcd given in Table I by using $\Delta H^{*}$ caled $=$ $\Delta G^{*}{ }_{\text {calcd }}+T \Delta S_{\text {caled }}^{*}$.

It is seen that both $\Delta H^{*}{ }_{\mathrm{pe}}$ and $\Delta H^{*}{ }_{\mathrm{rc}}$ are uniformly smaller than the corresponding values of $\Delta H^{*}{ }_{\text {calcd }}$ by amounts varying from ca. 0.5 to $2 \mathrm{kcal} \cdot \mathrm{mol}^{-1}$. Since the estimates of $\Delta H^{*} \mathrm{in}^{\text {a }}$ are likely to be correct within at least ca. $0.5 \mathrm{kcal} \cdot \mathrm{mol}^{-1}$, it seems likely that these discrepancies are due chiefly to theoretical estimates of the outer-shell component $\Delta H^{*}$ out that are somewhat too large.

Nonetheless, if we assume for the moment that the theoretical reorganization parameters $\Delta G^{*}$ calcd or $\Delta S^{*}$ calcd given in Table I are correct, these quantities can be combined with the experimental rate constants $k$ given in Table $\mathrm{II}^{14}$ to yield "experimental" estimates of the frequency factors $A_{\mathrm{a}}$ and $A_{\mathrm{b}}$ by using the relation

$$
\begin{equation*}
k=A_{\mathrm{a}} \exp \left(-\Delta G_{\mathrm{calcd}}^{*} / R T\right) \tag{7a}
\end{equation*}
$$

or

$$
\begin{equation*}
k=A_{\mathrm{b}} \exp \left(-\Delta H^{*} / R T\right) \exp \left(\Delta S_{\mathrm{calcd}}^{*} / R\right) \tag{7b}
\end{equation*}
$$

where $\Delta H^{*}$ in eq 7 b is obtained from the experimental Arrhenius slope (most simply by assuming that $A_{\mathrm{b}}$ is independent of temperature; i.e., $\Delta H^{*}=\Delta H^{*}$ ). The resulting values of $A_{\mathrm{a}}$ and $A_{\mathrm{b}}$ are listed in Table III, along with the frequency factors $A^{\mathrm{pe}}{ }_{\text {calcd }}$ and $A^{\mathrm{rc}}$ calcd calculated from the conventional forms of the preequilibrium and reactive collision models given by eq 8 and 9 , respectively: ${ }^{2,3}$

$$
\begin{align*}
& A_{\mathrm{calcd}}^{\mathrm{pe}}=\nu_{\mathrm{p}} K_{\mathrm{p}}^{\circ} \exp (-w / R T)= \\
& \qquad\left(\frac{\nu_{\mathrm{in}}^{2} \Delta G_{\mathrm{in}}^{*}}{\Delta G^{*}{ }_{\mathrm{calcd}}}\right)^{1 / 2} \frac{4 \pi N r^{3}}{3000} \exp (-w / R T)  \tag{8}\\
& A_{\mathrm{calcd}}^{\mathrm{cc}}=Z \exp (-w / R T)= \\
& \quad\left(N / 10^{3}\right)\left[8 \pi k_{\mathrm{B}} T\left(m_{1}+m_{2}\right) / m_{1} m_{2}\right]^{1 / 2} r^{2} \exp (-w / R T) \tag{9}
\end{align*}
$$

where $N$ is Avogadro's number, $m_{1}$ and $m_{2}$ are the masses of the

[^3]Table IV. Comparison of "Experimental" and Calculated Free Energies and Entropies of Activation for the Self-Exchange of $\operatorname{Bis}\left(\eta^{6}\right.$-arene $)$ chromium(I) $/(0)$ in $\mathrm{Me}_{2} \mathrm{SO}$ at $22^{\circ} \mathrm{C}$

| arene | act. free energies, $\mathrm{kcal} \cdot \mathrm{mol}^{-1}$ |  |  | act. entropies, cal $\cdot \mathrm{deg}^{-1} \cdot \mathrm{~mol}^{-1}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\overline{\Delta G^{*} \mathrm{pe}^{\text {a }}}$ | $\Delta G^{*} \mathrm{rc}^{\text {b }}$ | $\Delta G^{*}$ calcd $^{\text {c }}$ | $\overline{\Delta S^{*}{ }^{\text {pe }}{ }^{\text {d }}}$ | $\Delta S^{*}{ }_{\mathrm{rc}}{ }^{e}$ | $\Delta S^{*}$ calcd $^{f}$ |
| $\mathrm{C}_{6} \mathrm{H}_{6}$ | 6.4 | 5.0 | 6.1 | -8.1 | -4.4 | -1.0 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CH}_{3}$ | 7.0 | 5.2 | 5.2 | -8.1 | -3.1 | -0.9 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{OCH}_{3}$ | 6.6 | 4.7 | 6.2 | -10.1 | -4.9 | -1.2 |
| $\left(\mathrm{C}_{6} \mathrm{H}_{5}\right)_{2}$ | 6.5 | 4.4 | 4.4 | -13.2 | -7.1 | -0.9 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{COOC}_{2} \mathrm{H}_{5}$ | 6.0 | 4.0 | 4.3 | -12.1 | -7.0 | -0.8 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Cl}$ | 6.1 | 4.3 | 4.7 | -10.6 | -5.7 | -0.8 |

${ }^{a}$ Obtained from $\Delta G^{*}$ pe $=-R T \ln \left(k / A^{\mathrm{pe}}{ }_{\text {calcd }}\right)$. ${ }^{b}$ Obtained from $\Delta G^{*}{ }_{\mathrm{rc}}=-R T \ln \left(k / A^{\mathrm{rc}}\right.$ calcd $)$. ${ }^{c}$ Sum of $\Delta G^{*}$ out and $\Delta G^{*}$ in $(T)$; taken from Table 1. ${ }^{d}$ Obtained from $\Delta S^{*}{ }_{\mathrm{pe}}=\left(\Delta G^{*} \mathrm{pe}^{*}-\Delta H_{\mathrm{pc}}^{*}\right) / T ; \Delta H_{\mathrm{pe}}^{*}$ taken from Table II. ${ }^{e}$ Obtained from $\Delta S_{\mathrm{rc}}^{*}=\left(\Delta G^{*}{ }_{\mathrm{rc}}-\Delta H^{*} \mathrm{rc}\right) / T$; $\Delta H^{*}{ }_{\text {re }}$ taken from Table II. ${ }^{f}$ Sum of $\Delta S^{*}{ }_{\text {out }}$ and $\Delta S^{*}{ }_{\text {in }}(T)$; taken from Table I.
two reactants, $w$ is the electrostatic work required to form the collision complex from the separated reactants, and $\nu_{\text {in }}\left(\mathrm{s}^{-1}\right)$ is the effective frequency of the inner-shell motion (metal-ligand vibration); this was obtained from the symmetrical stretching frequencies $\nu_{0}$ and $\nu_{1}$ ( 270 and $279 \mathrm{~cm}^{-1}$, respectively) by using ${ }^{4} \nu_{\text {in }}$ $=c\left[2 \nu_{0}{ }^{2} \nu_{1}^{2} /\left(\nu_{0}^{2}+\nu_{1}^{2}\right)\right]^{1 / 2}$, where $c$ is the velocity of light. Since one of the reactants is uncharged, it is assumed that $w=0 .{ }^{14}$

Inspection of Table III reveals that the "experimental" frequency factors $A_{\mathrm{a}}$ are, in the majority of cases, close to (within a factor of 2) the values of $A^{\mathrm{rc}}$ cald, although ca. 5-20-fold smaller than $A^{\text {pe }}{ }_{\text {calcd }}$. The frequency factors $A_{\mathrm{b}}$ derived from the experimental rate constants and the activation energies along with $\Delta S^{*}$ calcd (eq 7 b ) are seen to be significantly smaller, ca. ${ }^{1} / 20$ of the corresponding values of $A_{\mathrm{a}}$ (Table III). These latter discrepancies result from the differences between the experimental and calculated values of $\Delta H^{*}$ (Table II), since the determination of $A_{\mathrm{a}}$ utilizes $\Delta G^{*}$ calcd, whereas the determination of $A_{\mathrm{b}}$ employs only the entropic component $\Delta S^{*}$ calcd (eq 7a,b). On the basis of the present evidence, it is difficult to decide whether $A_{\mathrm{a}}$ or $A_{\mathrm{b}}$ more closely approximates the true frequency factors; clearly, the choice depends upon whether $\Delta G^{*}$ calcd or $\Delta S^{*}{ }_{\text {calcd }}$ is considered more reliable. It has been suggested ${ }^{2}$ that the activation entropy $\Delta S^{*}$ can be taken as zero for self-exchange reactions since $\Delta S^{*}{ }_{\text {in }} \approx$ 0 and $\Delta S^{*}$ out is also predicted to be approximately zero from the dielectric continuum model. If indeed $\Delta S^{*} \approx 0$, then the smaller frequency factors $A_{\mathrm{b}}$ will be approximately correct. However, since the experimental activation enthalpies are smaller than the calculated values, it is likely that there would be a corresponding discrepancy between the actual and calculated activation entropies via a "compensation effect", ${ }^{15}$ so that $\Delta S^{*}<\Delta S^{*}$ calcd. For example, the effect could arise from an increase in specific solvent polarization required to form the transition state from the separated reactants, yielding an unexpected negative contribution to both $\Delta H^{*}$ and $\Delta S^{*}$. Consequently, the actual frequency factors may well be larger than $A_{\mathrm{b}}$ and close to $A_{\mathrm{a}}$. The latter corresponds to the situation in which the discrepancies between the actual and calculated enthalpic and entropic components of $\Delta G^{*}$ cancel, so that the actual free energies of activation approximately equal $\Delta G^{*}$ calcd.

The comparison between the predictions of the preequilibrium and collision models and the experimental kinetic parameters can equivalently be presented in terms of reorganization energies. Table IV contains values of free energies of activation $\Delta G^{*}{ }_{p e}$ and $\Delta G^{*}{ }_{\mathrm{rc}}$ obtained from the observed rate constants by using frequency factors calculated from the preequilibrium and collision models, respectively (eq 8 and 9). Listed alongside are the theoretical estimates $\Delta G^{*}$ calcd from Table I. It is seen that the corresponding values of $\Delta G^{*}{ }_{\mathrm{rc}}$ and $\Delta G^{*}$ calcd for most of the reactions agree closely (within $0.3 \mathrm{kcal} \cdot \mathrm{mol}^{-1}$ ), paralleling agreement between $A_{\mathrm{a}}$ and $A^{\mathrm{rc}}$ cald, , whereas the corresponding values of $\Delta G^{*}{ }_{\mathrm{pe}}$ are significantly ( $1.5-2 \mathrm{kcal} \cdot \mathrm{mol}^{-1}$ ) larger. Similar results have been obtained previously for several other outer-sphere self-exchange reactions. ${ }^{2-5}$ Table IV also contains estimates of activation entropies $\Delta S^{*}{ }_{\mathrm{pe}}$ and $\Delta S^{*}{ }_{\mathrm{rc}}$ obtained by combining the observed

[^4] 1125.


Figure 1. Plot of logarithm of rate constant $k$ for self-exchange of $\mathrm{Cr}\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{C}_{6} \mathrm{H}_{5}\right)_{2}{ }^{+/ 0}$ in various solvents vs. $1 / D_{\text {op }}-1 / D_{\mathrm{s}}$, where $D_{\text {op }}$ and $D_{\mathrm{s}}$ are the optical and static dielectric constants for each solvent: $1,9 / 1$ (v/v) $\mathrm{C}_{6} \mathrm{H}_{6} / \mathrm{CH}_{3} \mathrm{OH} ; 2$, benzonitrile; 3, dimethyl sulfoxide; 4, dimethylformamide; $5, \mathrm{I} / 4(\mathrm{v} / \mathrm{v}) \mathrm{C}_{6} \mathrm{H}_{6} / \mathrm{CH}_{3} \mathrm{OH}$; 6 , propylene carbonate; 7, $1 / 7(\mathrm{v} / \mathrm{v}) \mathrm{C}_{6} \mathrm{H}_{6} / \mathrm{CH}_{3} \mathrm{OH}$. Values of $k$ given in Table V ; sources for $D_{\text {op }}$ and $D_{\mathrm{s}}$ given in footnote $h$ to Table V.
rate constants and activation energies along with $A^{\text {pe }}$ calcd and $A^{\mathrm{rc}}$ calcd. It is seen that the values of $\Delta S^{*}$ rc are uniformly 3-6 eu more negative than $\Delta S^{*}$ calcd, which follows since $A_{\mathrm{b}}<A_{\mathrm{a}}, A^{\mathrm{rc}}$ calcd (Table III). The values of $\Delta S^{*}{ }_{p e}(-8$ to $-13 \mathrm{eu})$ seem unreasonably negative; a large increase in the extent of solvent ordering in the transition state compared to that for the separated reactants seems unlikely for the present systems. Consequently, it appears that the values of $A^{\mathrm{rc}}$ calded listed in Table III are too large.

Another method of estimating the frequency factor involves monitoring the rate constant for a given exchange reaction in several solvents. Since we can write

$$
\begin{equation*}
k=A \exp \left[-\left(\Delta G_{\text {in }}^{*}+\Delta G_{\text {out }}^{*}\right) / R T\right] \tag{10}
\end{equation*}
$$

if $\Delta G^{*}$ out is given by the dielectric continuum model (eq 5 ), then $\log k=$

$$
\begin{equation*}
\log A-\Delta G_{\mathrm{in}}^{*} / 2.303 R T-\frac{e^{2}}{2.303 \times 4 r R T}\left(\frac{1}{D_{\mathrm{op}}}-\frac{1}{D_{\mathrm{s}}}\right) \tag{11}
\end{equation*}
$$

Therefore, a plot of $\log k$ vs. $1 / D_{\text {op }}-1 / D_{\mathrm{s}}$ should allow $A$ to be obtained from the intercept, and $r$ from the slope. Such a plot is shown for the $\mathrm{Cr}\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{C}_{6} \mathrm{H}_{5}\right)_{2}{ }^{+/ 0}$ self-exchange reaction in seven solvents in Figure 1. The rate data are taken from ref 6 and were corrected for the effects of diffusion in the conventional manner by using $k^{-1}=k_{\text {app }}^{-1}-k_{\text {diff }}{ }^{-1}$, where $k_{\text {app }}$ is the measured (apparent) rate constant and $k_{\text {diff }}=8 R T / 3000 \eta$, where $\eta$ is the solvent viscosity. (This correction turned out to be small, yet significant in several solvents.) The values of $k$ are also listed in Table V .
It is seen that the variation of $k$ among most of the solvents studied is approximately in accord with eq 1 , suggesting that the

Table V. Rate Constants, Activation Parameters, and Experimental Frequency Factors $A\left(\mathrm{M}^{-1} \cdot \mathrm{~s}^{-1}\right)$ for the Self-Exchange of $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{C}_{6} \mathrm{H}_{5}\right)_{2} \mathrm{Cr}^{\mathrm{I} / 0}$ in Various Solvents at $22^{\circ} \mathrm{C}$

| solvent | $\begin{aligned} & 10^{-8} k,{ }^{a} \\ & \mathrm{M}^{-1} \cdot \mathrm{~s}^{-1} \end{aligned}$ | act. enthalpies, $\mathrm{kcal} \cdot \mathrm{mol}^{-1}$ |  |  | act. entropies, $\mathrm{cal} \cdot \mathrm{deg}^{-1} \cdot \mathrm{~mol}^{-1}$ |  |  | "exptl" freq factors, $\mathrm{M}^{-1} \cdot \mathrm{~s}^{-1}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | d $^{*}{ }^{\text {pe }}{ }^{\text {b }}$ | $\Delta H^{*} \mathrm{rc}^{c}$ | $\Delta H^{*}$ calcd $^{\text {d }}$ | $\overline{\Delta S^{*}{ }_{\text {pe }}{ }^{e}}$ | $\Delta S^{*}{ }_{\mathrm{rc}}{ }^{f}$ | $\Delta S^{*}$ calcd $^{\text {g }}$ | $\overline{A_{\mathrm{a}}(\mathrm{eq} 7 \mathrm{a})^{h}}$ | $A_{\mathrm{b}}(\mathrm{eq} 7 \mathrm{~b})^{h}$ |
| 9/1 (v/v) $\mathrm{C}_{6} \mathrm{H}_{6} / \mathrm{CH}_{3} \mathrm{OH}$ | 6.4 | 2.3 | 2.0 |  | -12.6 | -6.4 |  | $2.1 \times 10^{11}$ |  |
| benzonitrile | 4.1 | 2.7 | 2.4 | 3.8 | -11.9 | -6.1 | -1.4 | $4.2 \times 10^{11}$ | $7.7 \times 10^{10}$ |
| dimethyl sulfoxide | 2.5 | 2.6 | 2.3 | 4.2 | -13.2 | -7.4 | -0.9 | $4.5 \times 10^{11}$ | $3.1 \times 10^{10}$ |
| dimethylformamide | 2.2 | 3.1 | 2.8 | 4.1 | -11.5 | -5.8 | -1.9 | $5.5 \times 10^{11}$ | $1.0 \times 10^{11}$ |
| $1 / 4(v / v) \mathrm{C}_{6} \mathrm{H}_{6} / \mathrm{CH}_{3} \mathrm{OH}$ | 1.6 | 3.7 | 3.4 |  | -10.2 | -4.4 |  | $6.8 \times 10^{11}$ |  |
| propylene carbonate | 1.6 | 3.9 | 3.6 | 4.5 | -9.5 | -3.7 | -0.8 | $5.0 \times 10^{11}$ | $1.7 \times 10^{11}$ |
| $1 / 7(\mathrm{v} / \mathrm{v}) \mathrm{C}_{6} \mathrm{H}_{6} / \mathrm{CH}_{3} \mathrm{OH}$ | 1.2 | 3.8 | 3.5 |  | -10.2 | -4.7 |  | $5.8 \times 10^{11}$ |  |

${ }^{a}$ Experimental rate constant corrected for diffusion (see text), using viscosity data given in ref 21 . bbtained from experimental activation energy $E_{\mathrm{a}}$ assuming that $\Delta H^{*}{ }_{\mathrm{pe}}=E_{\mathrm{a}}$. ${ }^{c}$ Obtained from $E_{\mathrm{a}}$ assuming that $\Delta H^{*}{ }_{\mathrm{rc}}=E_{\mathrm{a}}-0.5 R T$. ${ }^{d}$ Obtained as in Table II, using dielectric constants from sources given in footnote $h$. ${ }^{e}$ Obtained from experimental rate constant and $A^{\text {pe }}$ calcd (eq (8)) as described in footnotes to Table IV. $f$ Obtained from experimental rate constant and $A^{\text {rc }}$ calcd (eq 9) as described in footnotes to Table IV. g Obtained as in Table IV, using dielectric constants from sources given in footnote $h$. $h$ Dielectric constant data required for calculating $\Delta G^{*}$ calcd (eq 7 a ) and $\Delta S^{*}$ calcd (eq 7 b ) obtained from following: $D_{\mathrm{op}}$ and $D_{\mathrm{s}}$ for benzene/methanol mixtures obtained by linear interpolation of values for pure solvents. Values of $D_{o p}$ for each solvent obtained from ref 22, except for propylene carbonate, given in: Simeral, L.; Amey, R. L. J. Phys. Chem. 1970, 74, 1443. Sources for $D_{\mathbf{s}}$ : Benzene, methanol, dimethyl sulfoxide: ref 21. Benzonitrile: Maryott, A. A.; Smith, E. R. Natl. Bur. Stand. (U.S.) Circ. 1951, No. 514. Dimethylformamide: Bass, S. J.; Nathan, W. I.; Meighan, R. M.; Cole, R. H. J. Phys. Chem. 1964, 68, 590. Propylene carbonate: Payne, R.; Theodorou, I. E. Ibid. 1972, 76, 2892.
dielectric continuum model provides a reasonable description of the solvent influence upon $\Delta G^{*}$. The straight line drawn through the points has a slope of 3.9 and a $y$ intercept of 10.1 . The resulting value of $r, 15.5 \AA$, is roughly comparable to the value, $11.6 \AA$ (Table I), deduced from the reactant structure by assuming a side-by-side configuration in the transition state. If we assume that $\Delta G^{*}{ }_{\text {in }}=1.3 \mathrm{kcal} \cdot \mathrm{mol}^{-1}$ (Table I), a frequency factor $A$ of ca. $9 \times 10^{10} \mathrm{M}^{-1} . \mathrm{s}^{-1}$ is obtained. Considering the lengthy extrapolation of Figure 1 necessary to determine $A$, the value is in reasonable agreement with $A_{\mathrm{a}}, A_{\mathrm{b}}$, and also $A^{\mathrm{rc}}$ calcd but again is markedly smaller than $A^{\text {pe }}$ calcd (Table III).

Table V also contains values of $A_{\mathrm{a}}$ and $A_{\mathrm{b}}$, determined for the self-exchange of $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{C}_{6} \mathrm{H}_{5}\right)_{2} \mathrm{Cr}^{1 / 0}$ in each solvent, which were obtained from the experimental data as in Table III. As expected, the values of $A_{\mathrm{a}}$ are largely independent of the solvent, although the values of $A_{\mathrm{b}}$ do vary somewhat and are $1 / 3$ to $1 / 15$ of those of $A_{\mathrm{a}}$. This variation of $A_{\mathrm{b}}$ with the solvent most likely arises from a solvent dependence of the outer-shell entropy term $\Delta S^{*}$ out which is larger than calculated by using the dielectric continuum model. However, it is seen from the values of $\Delta H^{*}{ }_{\mathrm{pe}}$ and $\Delta H_{\mathrm{rc}}{ }^{\mathrm{c}}$, also listed in Table V , that the major part of the solvent dependence of $k$ arises from variations in the enthalpic component, as predicted from theory.

Since the collision model yields frequency factors that are in closer agreement with the experimental results than are the frequency factors obtained from the simple preequilibrium model, it might be inferred that the former model provides a more accurate description of the physical events leading to electron transfer, i.e., that outer-sphere electron transfer is consummated by collision between suitably activated reactants rather than by vibronic excitation within a preformed bimolecular assembly. However, such a conclusion may be unwarranted. Both $A^{\text {pe }}$ calcd and $A^{\mathrm{rc}}$ calcd were calculated by assuming that the reactions are adiabatic, i.e., that $\kappa=1$. Some recent calculations ${ }^{4,16}$ indicate that substantially nonadiabatic pathways ( $\kappa \sim 10^{-3}-10^{-2}$ ) may predominate even for $\mathrm{Fe}\left(\mathrm{OH}_{2}\right)_{6}{ }^{3+/ 2+}$. Values of $\kappa$ below unity for the present system would tend to bring $A^{\mathrm{rc}}$ calcd into closer agreement with $A_{\mathrm{a}}$ and $A_{\mathrm{b}}$. A related point is that a steric factor arising from the nonspherical shape of the reactants should probably be included in the overall frequency factor. This contention is supported by the observation that both $A_{\mathrm{a}}$ and $A_{\mathrm{b}}$ fall significantly as substituents are added to the arene rings, to an extent that is greater for larger substituents (Table III). Thus the values of both $A_{\mathrm{a}}$ and $A_{\mathrm{b}}$ for $\mathrm{Cr}\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{C}_{6} \mathrm{H}_{5}\right)_{2}{ }^{+/ 0}$ self-exchange are about 4 -fold less than those for $\mathrm{Cr}\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)_{2}{ }^{+/ 0}$, even though the values of $A^{\text {pe }}{ }_{\text {calcd }}$ and $A^{\text {rc calcd }}$ are slightly greater for the latter

[^5]reaction. Even the parent arene reactants $\mathrm{Cr}\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)_{2}{ }^{+/ 0}$ are not spherical; reaction may occur preferentially, for example, with the arene rings in a "side-by-side" rather than "vertically stacked" configuration. ${ }^{6,17}$ Such steric selectivity would yield smaller values of $A^{\mathrm{pe}}$ calcd and $A^{\mathrm{rc}}$ calcd than obtained by using the conventional formulas (eq 8 and 9 ) which refer to spherical structureless reactants.

Further, the expression previously used ${ }^{2-5}$ for the precursor "stability constant" $K_{\mathrm{p}}=\left(4 \pi N r^{3} / 3000\right) \exp (-w / R T)$, appearing in eq 8, may yield incorrectly large estimates of $K_{\mathrm{p}}$ and hence $A^{\mathrm{pe}}{ }_{\text {calce }}$. This expression refers to the formation of contact pairs between two spherical species. It seems more appropriate to visualize $K_{\mathrm{p}}$ as being the probability of one reactant being within a given inclusion volume surrounding the other reactant within which electron transfer can occur. Most simply, the magnitude of this volume can be determined by

$$
\begin{equation*}
K_{\mathrm{p}}=\left[4 \pi N\left(d_{2}{ }^{3}-d_{1}{ }^{3}\right) / 3000\right] \exp (-w / R T) \tag{12}
\end{equation*}
$$

where $d_{1}$ is the minimum (contact) distance between the reactants and $d_{2}$ is the maximum distance on which electron tunneling can effectively occur. If, for example, $d_{2}-d_{1}=1 \AA$, eq 1 leads to values of $K_{\mathrm{p}}$ and hence $A^{\text {pe }}{ }_{\text {calcd }}$ for the present systems that are factors of $2-3$ smaller than those obtained with eq 8 . However, in reality $K_{\mathrm{p}}$ will continuously decrease as the internuclear distance increases rather than exhibit the discontinuity that is presumed in eq $12 .{ }^{19}$ Substantially smaller ( $\gtrsim 10$-fold) values of $K_{\mathrm{p}}$ can also be deduced by using this model by taking into account the nonsphericity of the reactants and assuming that only certain precursor structures, such as a "side-by-side" configuration, result in electron transfer.
Consequently, the values of $A^{\text {pe }}{ }_{\text {calcd }}$ obtained by taking such steric and tunneling factors into account could become comparable to the experimental estimates of $A_{\mathrm{a}}$ and $A_{\mathrm{b}}$. Also, the apparently good agreement seen between $A^{p c}$ calcd and $A_{\mathrm{a}}$ and $A_{\mathrm{b}}$ is probably misleading since the inclusion of reasonable steric factors for the present reactants into the collisional model (eq 9) would almost certainly yield values of $A^{\text {pe }}$ calcd which are markedly too small.

## Conclusions

By and large, the experimental kinetics parameters are in reasonable agreement with the predictions from conventional electron-transfer theory, at least if the collision model is used to provide estimates of the effective frequency factors. However,

[^6]it is interesting to note that the deviations observed between experiment and theory are qualitatively similar to those seen previously for other self-exchange reactions. Thus it has been found that $\Delta H^{*}<\Delta H^{*}$ calcd and $\Delta S^{*}<\Delta S^{*}$ calce for ferrocini$\mathrm{um} /$ ferrocene in a number of solvents. ${ }^{20}$ and for $\mathrm{Ru}\left(\mathrm{NH}_{3}\right)_{4}$ bpy ${ }^{3+/ 2+}$ in aqueous media. ${ }^{2}$ Most likely, these discrepancies reflect a limitation of the dielectric continuum model, possibly arising from changes in short-range reactant-solvent interactions required to form the encounter complex "solvent cage" prior to electron transfer. The requirement of forming a particular encounter geometry, with the two reactants essentially in contact so as to
(20) Yang, E. S.; Chan, M.-S.; Wahl, A. C. J. Phys. Chem. 1980, 84, 3094. Also see: Chan, M.-S.; Wahl, A. C. J. Phys. Chem. 1982, 86, 127. (21) Janz, G. J.; Tomkins, R. P. T. "Nonaqueous Electrolyte Handbook"; Academic Press: New York, 1972; Vol. I.
(22) Riddick, J. A.; Bunger, W. B. "Organic Solvents"; Wiley-Interscience: New York, 1970.
maximize the transmission coefficient, may partly be responsible for the experimental frequency factors being markedly smaller than those calculated that a simple model involving activation of a precursor complex formed in a prior equilibrium step. However, the simple collision model appears to have greater practical utility for outer-sphere processes, at least for the purpose of making numerical calculations.

Acknowledgments. We are grateful to Dr. Norman Sutin for critically reading the manuscript and making several helpful suggestions. This work was supported in part by the Office of Naval Research.

Registry No. $\left(\eta^{6}-\mathrm{C}_{6} \mathrm{H}_{6}\right)_{2} \mathrm{Cr}^{1}$, 11077-47-7; $\left(\eta^{6}-\mathrm{C}_{6} \mathrm{H}_{6}\right)_{2} \mathrm{Cr}^{0}$, 1271-54-1; $\left(\eta^{6}-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CH}_{3}\right)_{2} \mathrm{Cr}^{1}, 33505-50-9 ;\left(\eta^{6}-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CH}_{3}\right)_{2} \mathrm{Cr}^{0}$, $12087-58-0$; $\left(\eta^{6}-\right.$ $\left.\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{OCH}_{3}\right)_{2} \mathrm{Cr}^{1}, 75170-79-5 ;\left(\eta^{6}-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{OCH}_{3}\right)_{2} \mathrm{Cr}^{0}, 57820-92-5 ;\left(\eta^{6}-\right.$ $\left.\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{C}_{6} \mathrm{H}_{5}\right)_{2} \mathrm{Cr}^{1}$, $33154-48-2 ;\left(\eta^{6}-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{C}_{6} \mathrm{H}_{5}\right)_{2} \mathrm{Cr}^{0}, 33085-81-3 ;\left(\eta^{6}-\right.$ $\left.\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{COOC}_{2} \mathrm{H}_{5}\right)_{2} \mathrm{Cr}^{1}, 57219-88-2 ;\left(\eta^{6}-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{COOC}_{2} \mathrm{H}_{5}\right)_{2} \mathrm{Cr}^{0}$, $57219-87-1$; $\left(\eta^{6}-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Cl}\right)_{2} \mathrm{Cr}^{2}, 75170-75-1 ;\left(\eta^{6}-\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Cl}^{2}\right)_{2} \mathrm{Cr}^{0}, 42087-89-8$.

# Coordination Modes of Histidine. 3. ${ }^{1}$ Stereochemistry of Copper(II) Complexes Related to Pyridoxal Catalysis 

Luigi Casella,* Michele Gullotti, and Gianfranco Pacchioni<br>Contribution from the Istituto di Chimica Generale ed Inorganica dell'Università, Centro CNR, 20133 Milano, Italy. Received August 3, 1981


#### Abstract

Copper(II) complexes of Schiff bases derived from pyridoxal, salicylaldehyde, or pyruvic acid and histidine, histidine methyl ester, and representative amino acids with nonpolar side chains have been prepared by metal ion template synthesis. The mode of coordination to copper(II) of the histidine residues in these complexes has been investigated by circular dichroism spectroscopy. The complexes derived from amino acids with nonpolar side chains provide appropriate references for the glycine-like coordination mode, while the derivatives of histidine methyl ester are appropriate references for the histamine-like mode. The histidine residues exhibit a striking tendency to bind copper(II) through chelate ring types complementary to those of the fused carbonyl residue. Thus, in the complexes derived from pyridoxal and salicylaldehyde the histidine residues bind glycine-like, whereas in those derived from pyruvic acid the histidine residues bind histamine-like. The conformation of the coordinated Schiff base ligands has been deduced from the circular dichroism spectra of the complexes and discussed in relation to vitamin $\mathrm{B}_{6}$ model reactions. The EPR spectra of the complexes were also investigated in different solvents to establish the donor sets and the ligand field symmetry in solution. The spectra show the pattern typical for tetragonal symmetry ( $g_{\|}>g_{\perp}$ ), and the magnetic parameters were used to compute the molecular orbital coefficients that describe the bonding character in the complexes. The electronic excitation energies required in the calculations were deduced from the circular dichroism spectra.


Most of the transformations that amino acids undergo during metabolism are catalyzed by enzymes requiring pyridoxal phosphate as a cofactor. ${ }^{2}$ The mechanisms proposed for pyridoxal catalysis, however, have mostly been derived from studies on model systems utilizing amino acid-pyridoxal and related Schiff bases and their metal complexes. ${ }^{3,4}$ The work in this field has focused

[^7]on mechanistic and spectroscopic properties of the systems, and only recently the enhancement of reactivity of a group to the amino acid $\alpha$-carbon atom has been related to its correct stereochemical positioning within the molecule. ${ }^{5}$ As first suggested by Dunathan, ${ }^{6}$ an easy cleavage of a bond to the amino acid $\alpha$-carbon atom in I can be accomplished by orienting that bond orthogonal to the

plane of the extended $\pi$ system in order to optimize $\sigma-\pi$ overlap. This stereoelectronic requirement enables pyridoxal-dependent enzymes to achieve reaction specificity and enhance reaction rates by proper conformational orientation of the bond to be cleaved (or formed). Despite the importance of recognizing the stereochemical factors that control the correct positioning of the groups

[^8]
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